Chapter 8.2

Q1 $Q = CV = 12 \times 10^{-6} \times 24 = 2.9 \times 10^{-4}$ C.

Q2 The voltage at the ends of the capacitor is the same as that across the resistor.
Initially, the voltage is $V = \dfrac{Q}{C} = \dfrac{24 \times 10^{-9}}{2.0 \times 10^{-9}} = 12$ V and so the initial current will be

$I = \dfrac{V}{R} = \dfrac{12}{6.0} = 2.0$ A.

Q3 (a) $500 \times 500 \times 8 = 2 \times 10^{6}$ bits. (b) We need a 5 bit word:
($26 = 1 \times 2^{4} + 1 \times 2^{3} + 0 \times 2^{2} + 0 \times 2^{1} + 1 \times 2^{0} = 11001$). (c) For each word we need
$6 \times 5 = 30$ bits and so the number of words corresponding to 2×10^{6} bits is
$\dfrac{2 \times 10^{6}}{30} = 6.7 \times 10^{4} \approx 7 \times 10^{4}$. (d) According to this calculation the saying appears to
be true!

Q4 $E = hf = \dfrac{hc}{\lambda} = \dfrac{6.63 \times 10^{-34} \times 3.0 \times 10^{8}}{5.8 \times 10^{-7}} = 3.4 \times 10^{-19}$ J.

Q5 The area of each pixel is $\dfrac{36}{3.0 \times 10^{6}} = 1.2 \times 10^{-5}$ mm^{2} $= 1.2 \times 10^{-11}$ m^{2}. The linear
size is thus $\sqrt{1.2 \times 10^{-11}} = 3.5 \times 10^{-6}$ m .

Q6 Quantum efficiency is the ratio of the number of electrons emitted to the number
of photons incident on a pixel. Magnification is the ratio of the linear size of the
image on the CCD to the length of the object.

Q7 The fraction of photons ejecting electrons is 2/3 and the quantum efficiency is
67%.

Q8 (a) Resolution is the ability to see two different points on the object as different
points in the image. (b) The idea is not to have photons from two different points on
the object fall on the same pixel. A rough condition to achieve this is to demand that
photos from the two different points on the object fall on two different pixels with a
minimum of one pixel in between empty. This means that the images of the two
points must be separated by at least one pixel on the CCD.

Q9 Resolution has to do with the distance between adjacent pixels. For the same area
camera the one with the larger density of pixels will also have the smaller pixel
separation.

Q10 A digital camera (for personal use or cameras on telescopes and space based
telescopes), video camera, a copier, a scanner, a fax machine and X-ray detectors for
medical uses.

Q11 Light incident on the collecting area of the CCD causes electrons to be ejected from each pixel (by a process similar to the photoelectric effect) and hence a potential difference is established at the ends of each pixel. The potential difference is proportional to the charge in each pixel and that in turn is proportional to the intensity of light in each pixel. The potential difference is read sequentially, row by row and its value is first converted into binary (digital) form along with the position of each pixel. Knowing the position of each pixel and the intensity of light in each allows the construction of an image.

Q12 The large difference in the number of pixels means that the 8 megapixel camera consists of smaller pixels and so the separation of pixels is much smaller. This means that this camera will have a better resolution i.e. much finer detail in the images will be possible.

Q13 The advantage of a high quantum efficiency is that a shorter exposure time will be required.

Q14 There will not be any difference in the two images. The advantage of a larger collecting area is that a larger area can be imaged.

Q15 The ratio of the areas of image to object is $\dfrac{9.4 \times 10^{-6}}{6.2 \times 10^{-6}} = 1.516$. The magnification is the ratio of the linear size of the image to that of the object and is thus $\sqrt{1.516} = 1.23 \approx 1.2$.

Q16 The distance between the images of the two points will be $8.2 \times 10^{-4} \times 1.3 = 1.07 \times 10^{-3}$ mm. The area of one pixel is $\dfrac{16}{4.0 \times 10^{6}} = 4.0 \times 10^{-6}$ mm^2 and its linear size is $\sqrt{4.0 \times 10^{-6}} = 2.0 \times 10^{-3}$ mm. The distance between the images is less than two pixel sizes and so the images cannot be resolved.

Q17 (a) In 1 second the power incident on a unit area (1 square meter) is 28 J. The energy of one photon is $E = hf = \dfrac{hc}{\lambda} = \dfrac{6.63 \times 10^{-34} \times 3.0 \times 10^{8}}{6.8 \times 10^{-7}} = 2.9 \times 10^{-19}$ J and so the number of photons per unit time per unit area is $\dfrac{28}{2.9 \times 10^{-19}} = 9.7 \times 10^{19}$. (b) These photons have more energy and so fewer of them are required. Their number will be $9.7 \times 10^{19} \times \dfrac{4.4}{6.8} = 6.3 \times 10^{19}$.

Q18 (a) The energy of one photon is $E = hf = \dfrac{hc}{\lambda} = \dfrac{6.63 \times 10^{-34} \times 3.0 \times 10^{8}}{4.8 \times 10^{-7}} = 4.11 \times 10^{-19}$ J and so the energy of 6000 of them is $6000 \times 4.11 \times 10^{-19} = 2.47 \times 10^{-15}$ J. The energy given to the pixel is

$1.4 \times 10^{-3} \times 5.0 \times 10^{-10} \times t = 2.47 \times 10^{-15} \Rightarrow t = 3.5$ ms. (b) The quantum efficiency of the camera cannot be 100% and so not all of the 600 photons will be absorbed. To get the acceptable image therefore a longer time must be used to allow for more photons to be incident on the pixels.

Q19 The area of one pixel is $\dfrac{48}{4.0 \times 10^6} = 1.2 \times 10^{-5}$ mm^2 $= 1.2 \times 10^{-11}$ m^2. The energy of one photon is $E = hf = \dfrac{hc}{\lambda} = \dfrac{6.63 \times 10^{-34} \times 3.0 \times 10^8}{6.3 \times 10^{-7}} = 3.16 \times 10^{-19}$ J. The energy deposited in the pixel in 80 ms by N photons is thus
$N \times 3.16 \times 10^{-19} = 5.2 \times 10^{-3} \times 1.2 \times 10^{-11} \times 80 \times 10^{-3}$ and so $N = 2.8 \times 10^4$. Since the QE is 0.75 the number of electrons ejected in one pixel is
$N = 0.75 \times 2.8 \times 10^4 = 2.1 \times 10^4$ and hence the electric charge developed is
$2.1 \times 10^4 \times 1.6 \times 10^{-19} = 3.36 \times 10^{-15}$ C. Hence the voltage is
$V = \dfrac{Q}{C} = \dfrac{3.36 \times 10^{-15}}{24 \times 10^{-12}} = 1.4 \times 10^{-4}$ V.

Q20 The charge that develops in each row of pixels must be read and recorded. This is done by sequentially moving the charge in each row to the row below and the charge in the very last row to the register where it is measured. Thus the charge in each row is connected i.e. coupled to that in the row below.

Q21 The number is $\dfrac{5.0 \times 10^3}{3.65} = 1.4 \times 10^3$.

Q22 Advantages include:
- The image is digital and so can be edited/manipulated/electronically transported.
- Many more images may be stored in a digital camera than on film.
- The response of the CCD is uniform over a wide range of wavelengths (i.e. the number of electrons ejected is the same for the same number of photons of different wavelengths).
- The response of the CCD is fairly linear which means that the number of electrons ejected is proportional to the intensity of light. Faint as well as bright objects can appear on the same image.
- The noise is very limited (i.e. there is little charge created in the pixels whose origin is other than light incident on the pixel.

Q23 At higher temperatures there is considerable thermal motion of electrons. (Recall that temperature is proportional to the average random kinetic energy of molecules but also of electrons.) Hence at higher temperatures electrons may be ejected from the pixels and contribute to the potential difference at the ends of the pixels even when no light falls on the pixels. Lowering the temperature prevents that to a considerable degree.

Q24 The most important characteristic is the ability of the CCD to create at the same time an accurate image of a very faint and a very bright object. With photographic film the fainter image tends to wash out. Further, since the image is in digital form it can be easily processed and analyzed using various kinds of software. Finally, their small size allows their placement in spacecraft or orbiting stations. The digital nature of the image then allows the image to be sent down to earth.

Q25 It can be used to record X-rays with an exposure time that is much less than the conventional method using film. The short exposure time limits the radiation delivered to the patient.